

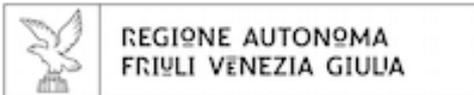
# Introduction to Particle Accelerators

*With Focus on Synchrotron Light Sources*

Simone Di Mitri

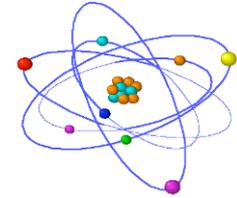
*Elettra Sincrotrone Trieste*

*University of Trieste, Dept. of Physics*



*The project is funded by the Italian Region Friuli Venezia Giulia, within the program "Regional plan for the building up of the formative offer for the academic year 2017/2018", in the section "Special projects"*

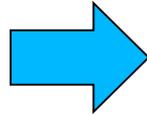
# Ingredients



- ❑ **Charged particles**: electrons, protons, ions, anti-particles

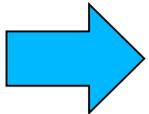
$$E = \gamma(v)m_0c^2$$

$$F_L = q(\vec{E} + \vec{v} \times \vec{B})$$



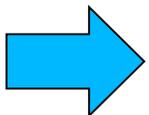
***Special Relativity*** is all we need. Includes kinematics and dynamics of relativistic charged particles.

- ❑ Static and time-varying **electric field** increases the particle kinetic energy.



***Radiofrequency (RF) accelerating structures***

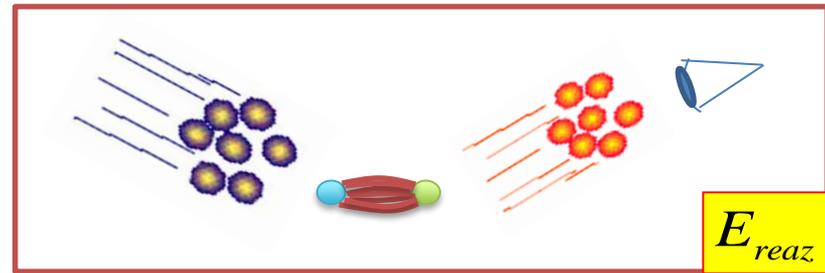
- ❑ Static and time-varying **magnetic field** bounds the particle inside the vacuum chamber.



***Magnetic elements*** for controlling the particles direction (orbit) and beam size (focusing).

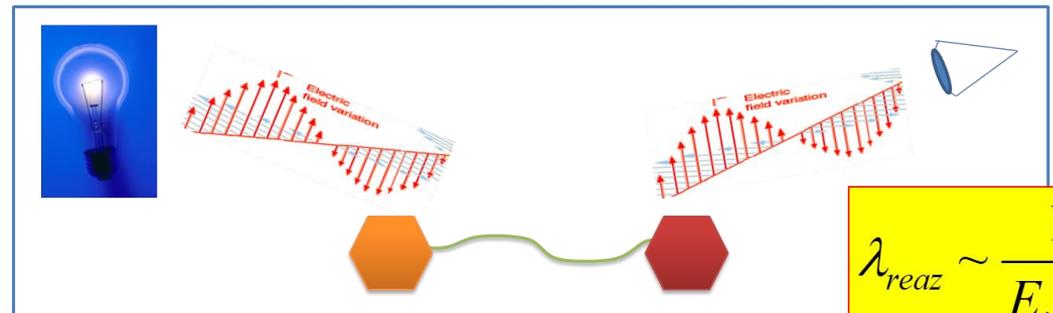
# Why High Energy Particle Beams ?

## “Colliders” (LHC,...)

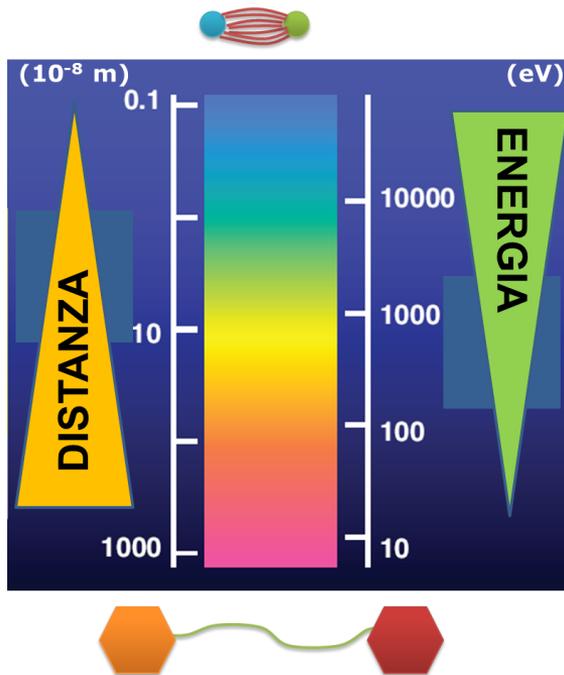


$$E_{\text{reaz}} \sim E_{\text{incid}}$$

## “Synchrotron Light Sources” (Elettra,...)



$$\lambda_{\text{reaz}} \sim \frac{1}{E_{\text{incid}}}$$

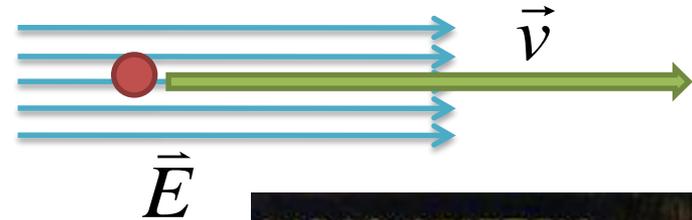


# Acceleration, Particle Energy

$$L = F \cdot \vec{s} = q\vec{E} \cdot \vec{s} = -q\Delta V$$

Electric field

Energy

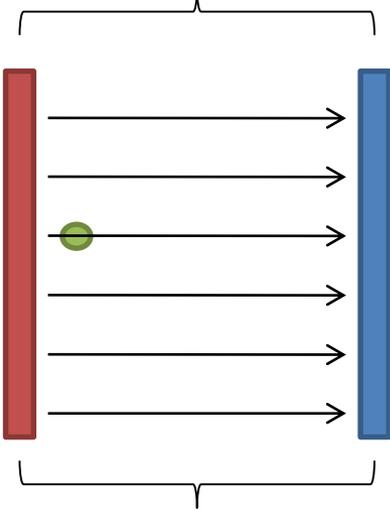


$\Delta V$

$$J = N \times m = C \times V$$

$$1 \text{ eV (electronvolt)} = 1 \text{ e} \times 1 \text{ V}$$

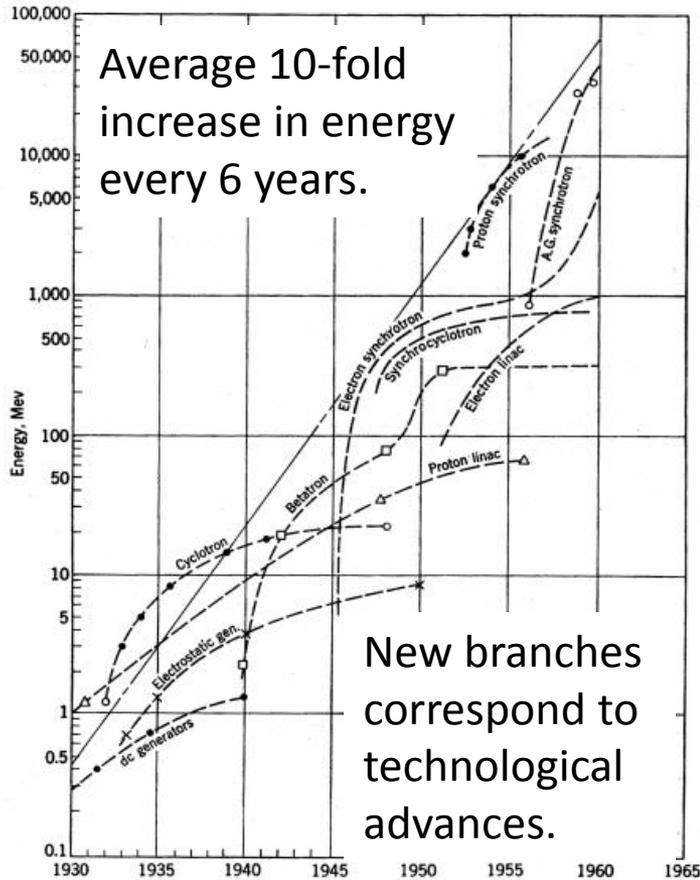
$$e = -1.6 \times 10^{-19} \text{ C}$$



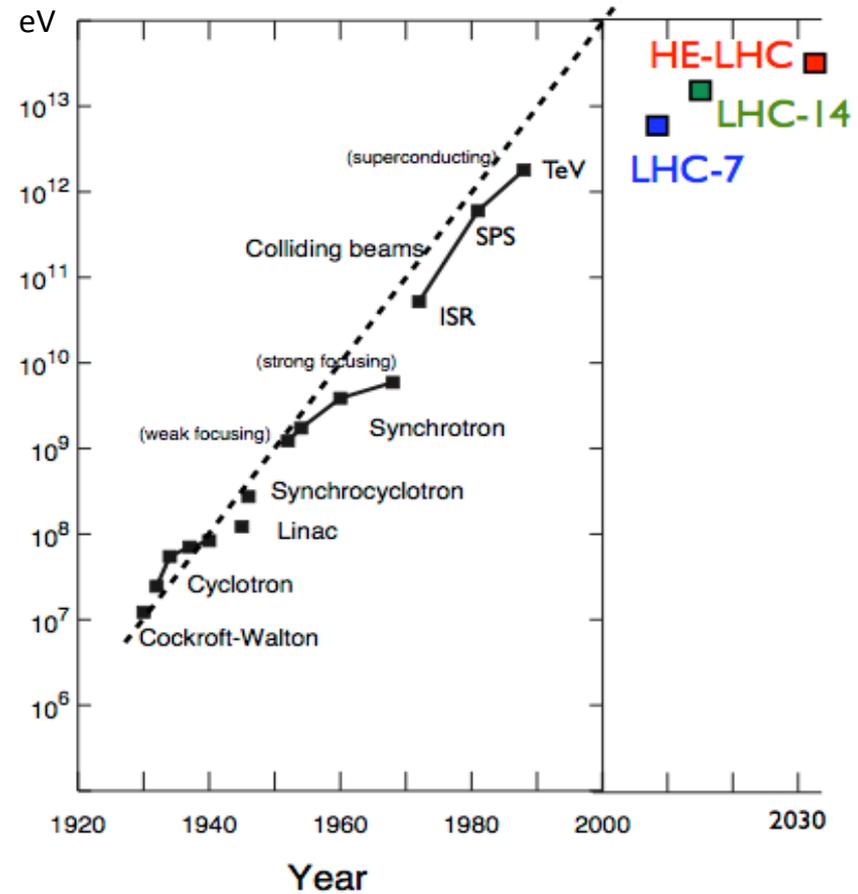
$$\Delta E = -q\Delta V$$



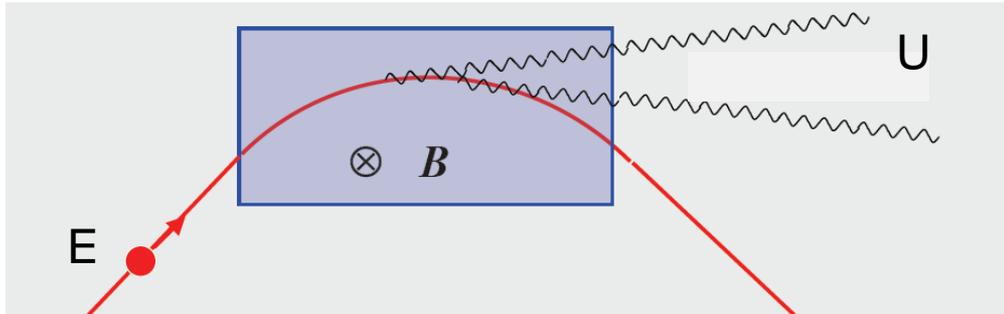
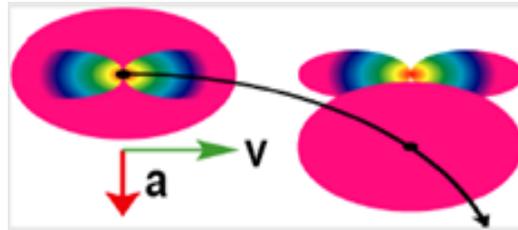
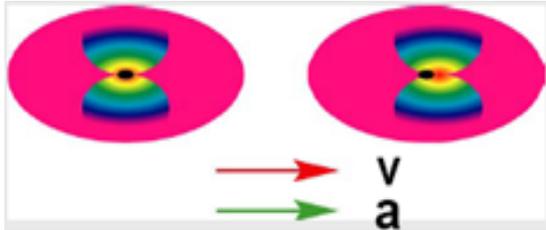
# Livingstone Chart



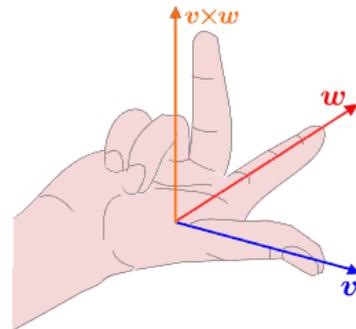
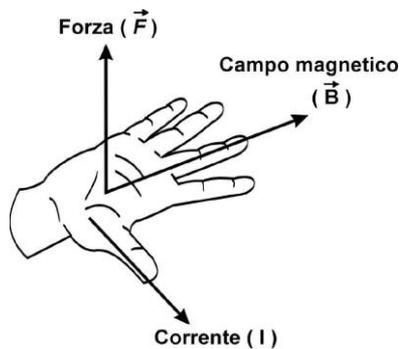
C.M. Energy (eV)



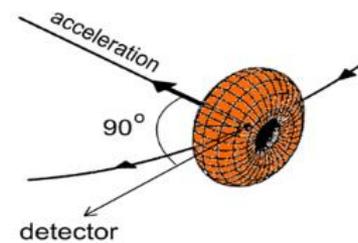
# Synchrotron Radiation



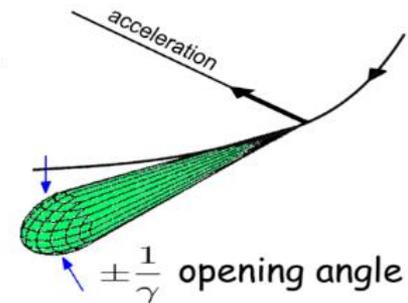
$$U_{turn} [keV] = 88.5 \frac{E_b^4 [GeV]}{R [m]}$$



Moving frame of electron

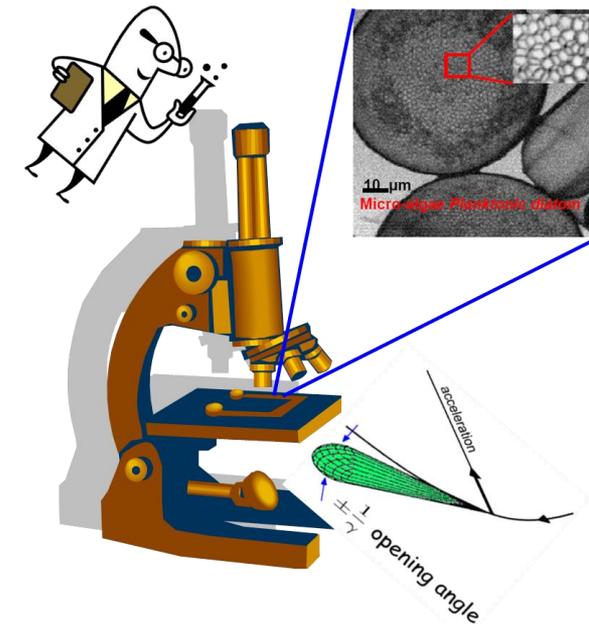
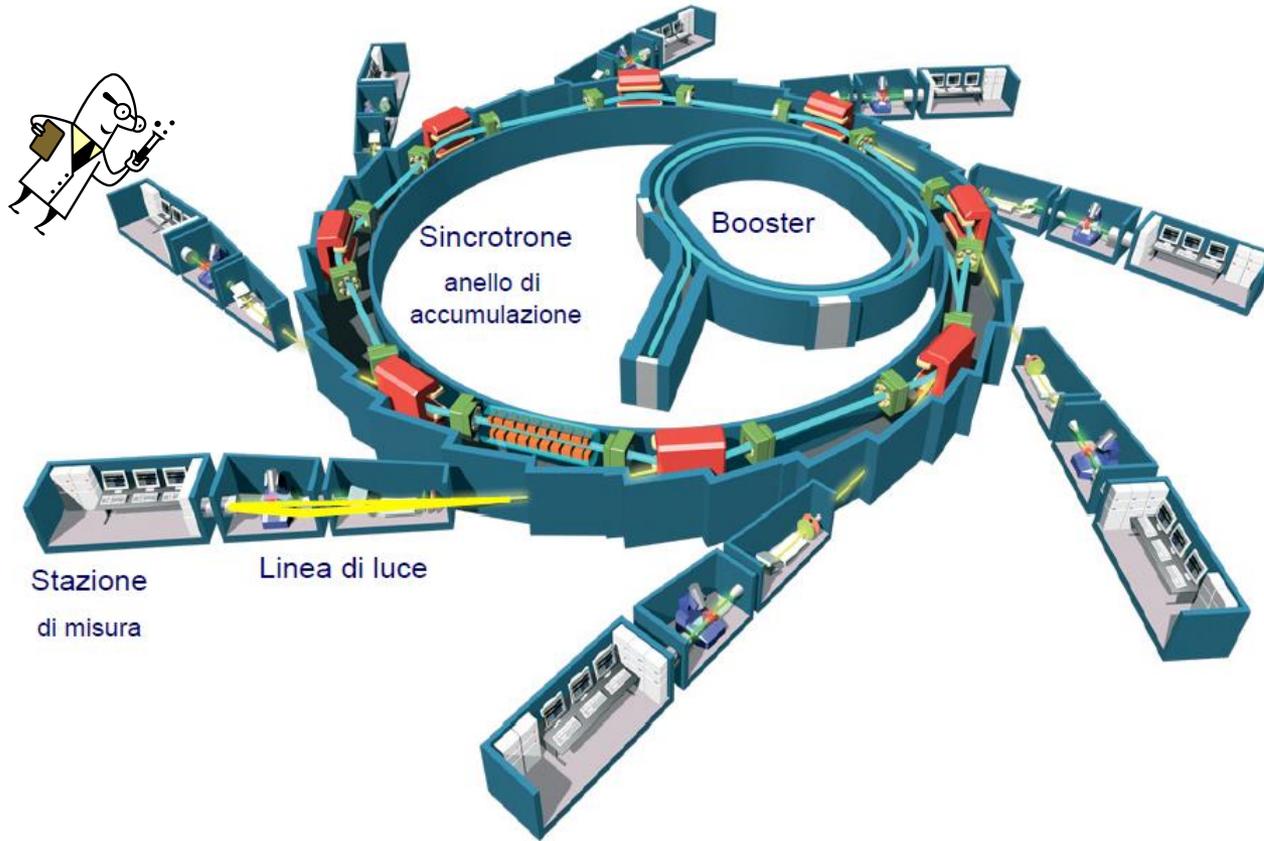


Lab frame



$$\frac{1}{\gamma} = \frac{m_0 c^2}{E} = \sqrt{1 - \left(\frac{v}{c}\right)^2}$$

# Synchrotron Light Source



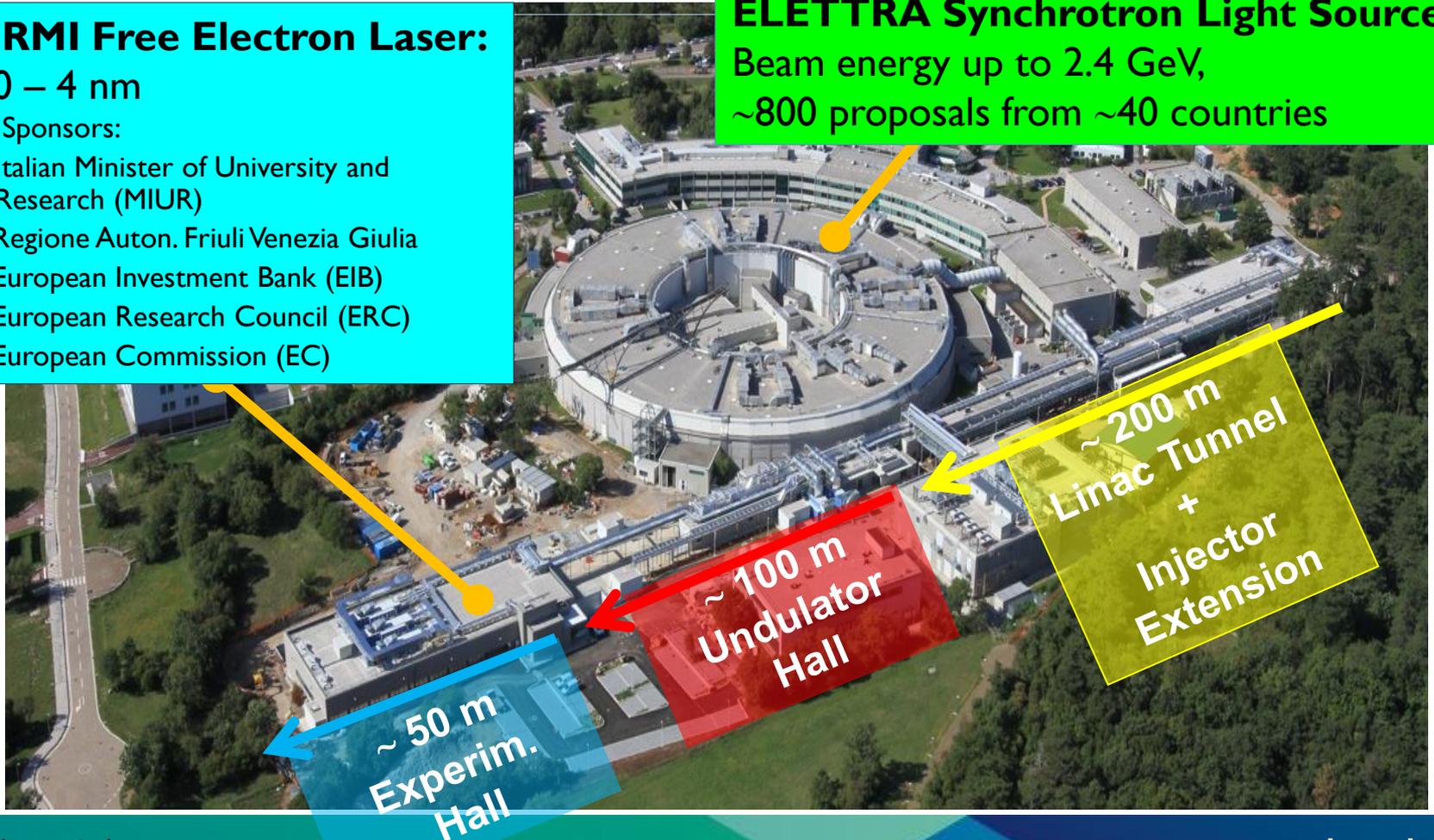
# Elettra Sincrotrone Trieste

Elettra Sincrotrone Trieste is a nonprofit shareholder company of Italian national interest, established in 1987 to construct and manage synchrotron light sources as international facilities.

## FERMI Free Electron Laser: 100 – 4 nm

- Sponsors:  
Italian Minister of University and Research (MIUR)  
Regione Auton. Friuli Venezia Giulia  
European Investment Bank (EIB)  
European Research Council (ERC)  
European Commission (EC)

**ELETTRA Synchrotron Light Source:**  
Beam energy up to 2.4 GeV,  
~800 proposals from ~40 countries

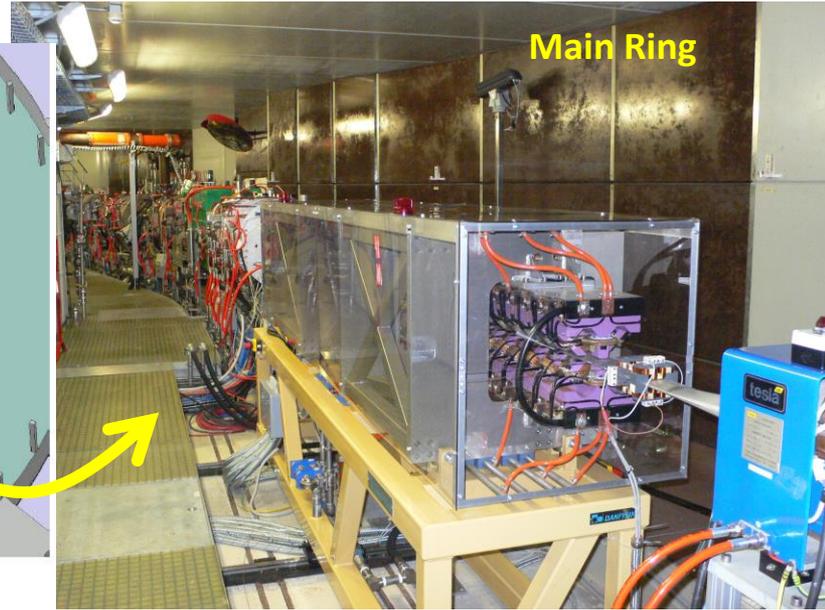
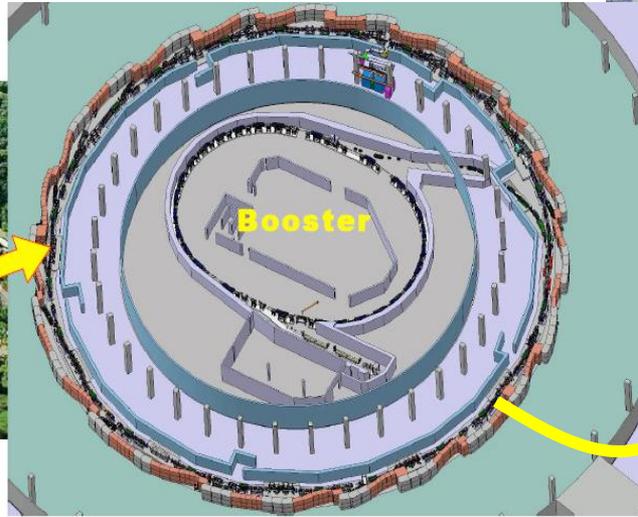
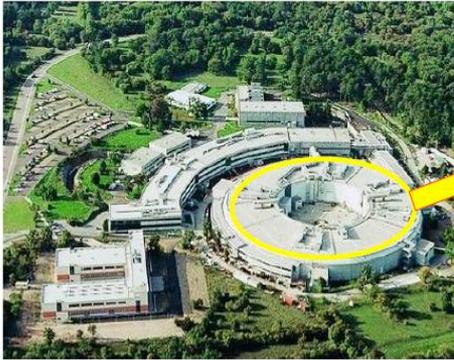


~ 200 m  
Linac Tunnel  
+  
Injector  
Extension

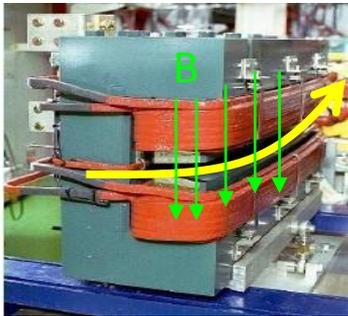
~ 100 m  
Undulator  
Hall

~ 50 m  
Experim.  
Hall

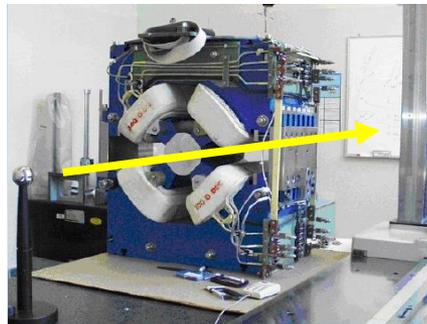
# Elettra Synchrotron Light Source



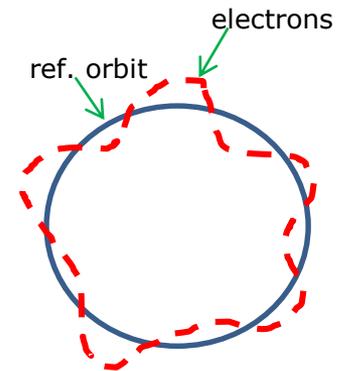
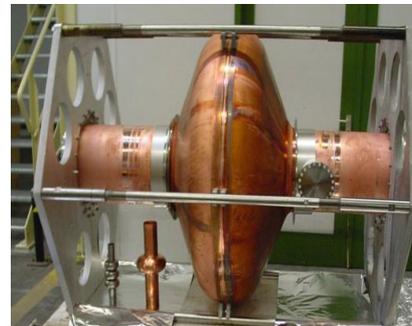
Dipole Magnet



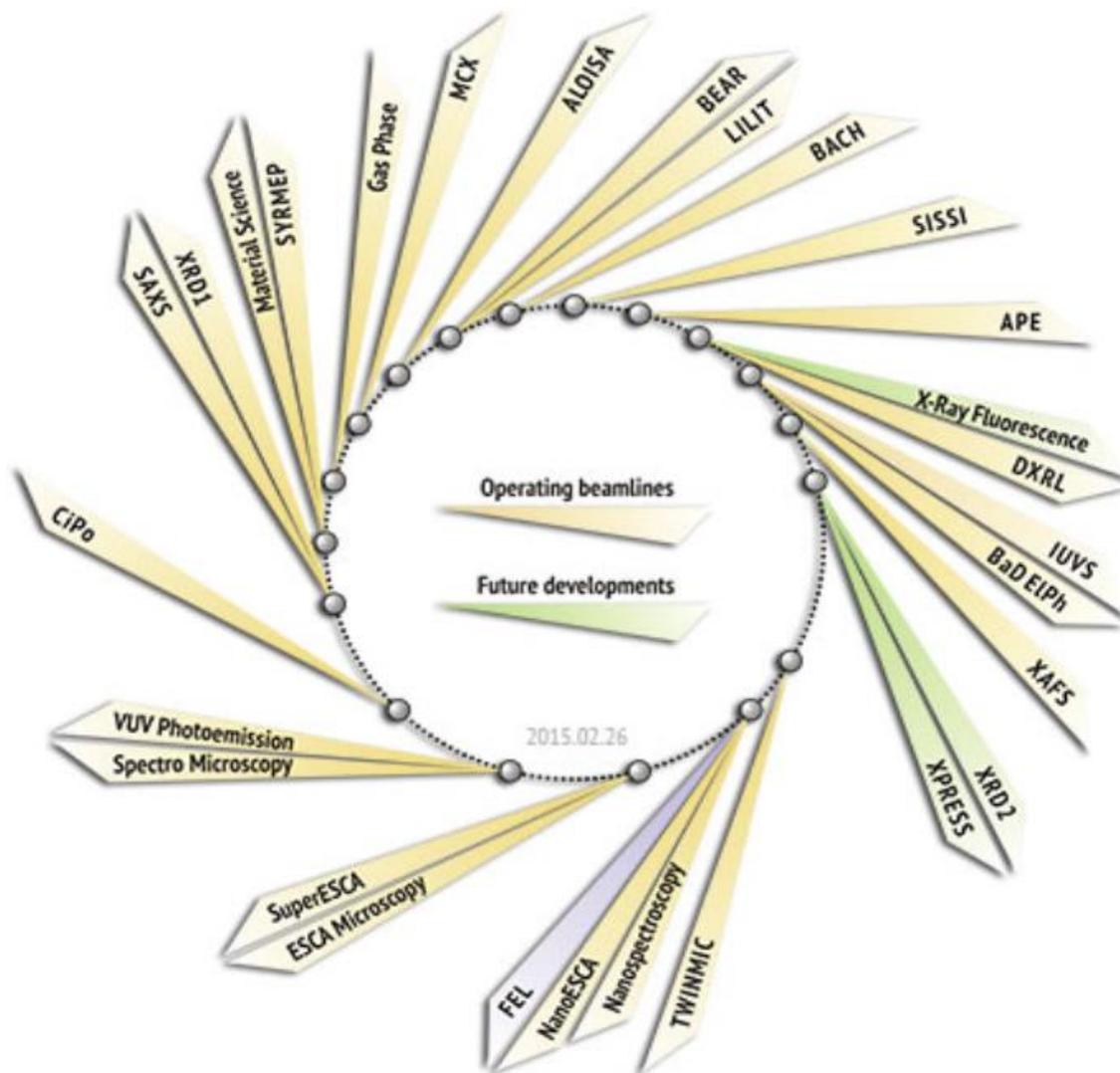
Quadrupole Magnet



RF cavity

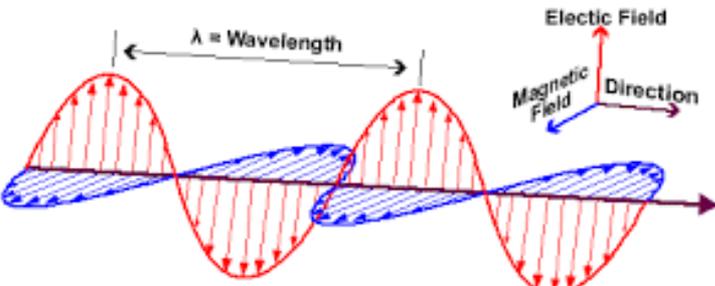
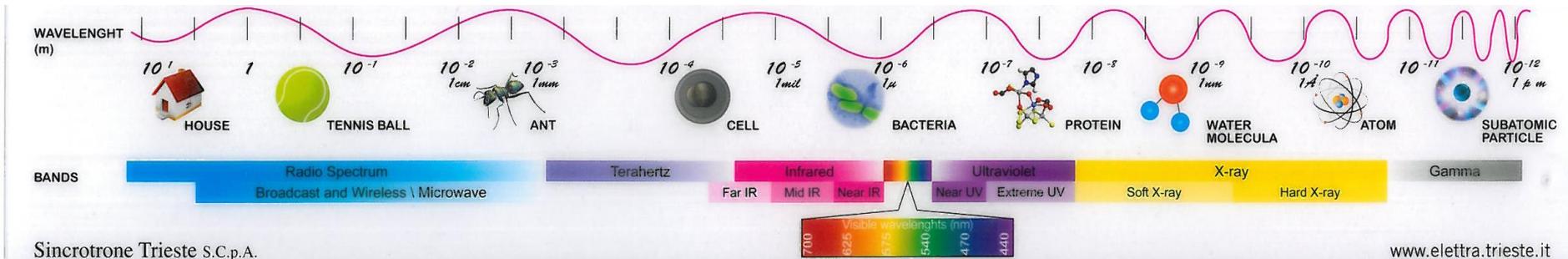


# Elettra Photon Beamlines



- 28 beamlines open to Users
- Physics of Matter, Biology, Chemistry, Medical Science, Technology Materials, Environment, etc...

# Wavelength, Photon Energy



$$c [m/s] = \lambda \cdot \nu$$

$$f [Hz] = 2\pi\nu$$

$$E [J] = h \cdot \nu$$

- An e.m. wave can be described also as a bunch of massless particles, named “photons”.
- Photons travel at speed  $c$  in vacuum.
- The energy of an e.m. wave (monochromatic) is the photon energy times the number of photons.

$c = 2.998e8 \text{ m/s}$

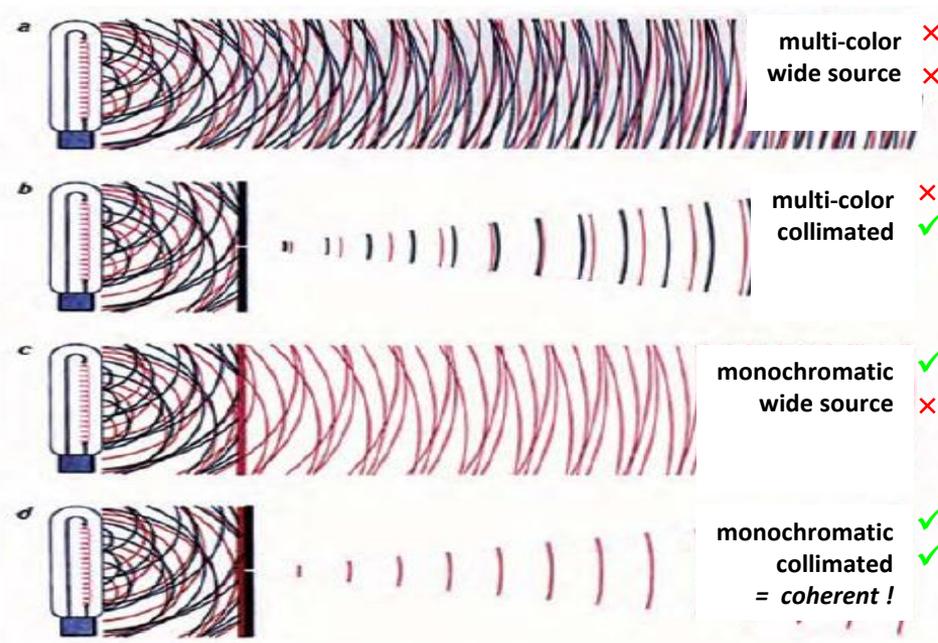
*Light speed in vacuum*

$h = 6.626e-34 \text{ J s}$

*Planck constant*

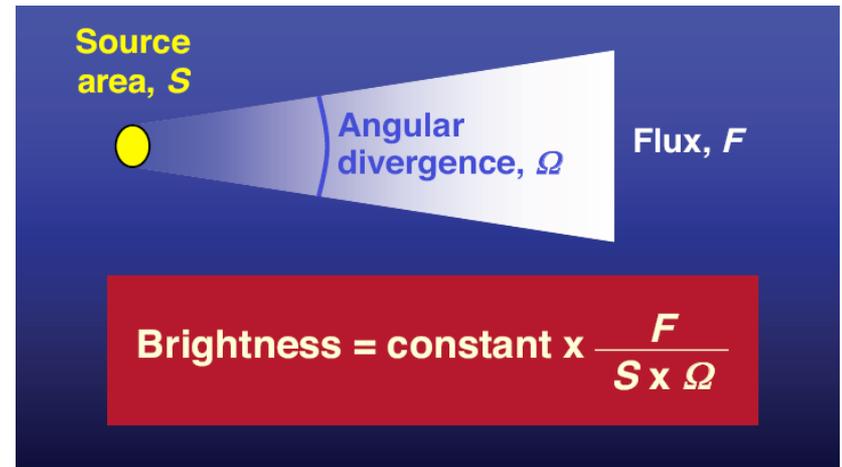
# Radiation Properties

## Transverse & Longitudinal Coherence

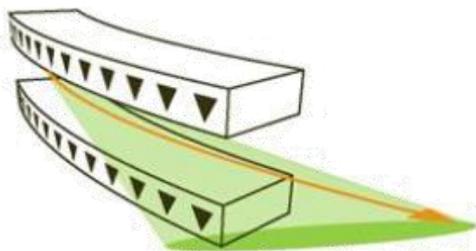


Courtesy of A. Schawlow, Stanford.

## Brilliance



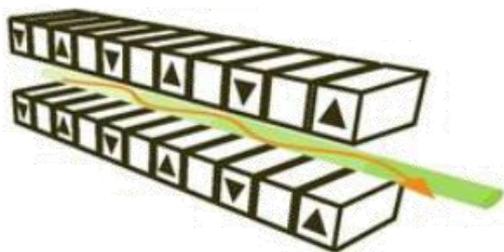
# Radiation Sources



## Magneti Curvanti

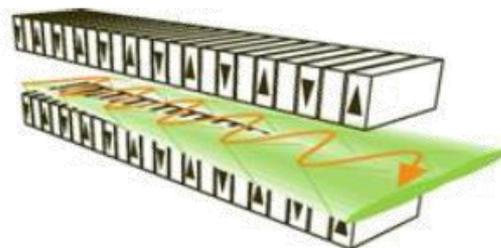
I magneti Curvanti mettono in connessione due sezioni diritte del sincrotrone: la luce è prodotta mediante la “bremsstrahlung radiations”.

I Magneti di Inserzione (straight sections) sono nelle sezioni diritte e producono radiazione più intensa: gli elettroni fanno un moto a zig-zag, emettendo luce.



## Ondulatore

La luce del raggio è coerente e collimata

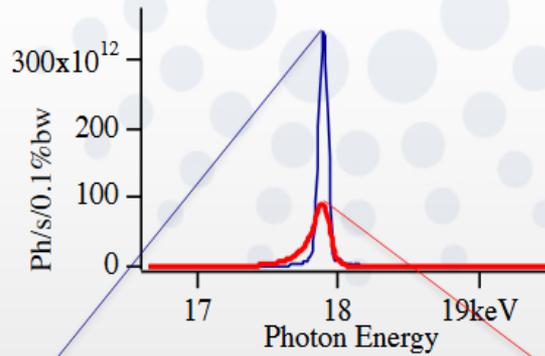


## Wiggler

La luce del raggio è incoerente e non collimata

# Spectral Flux

Undulator:  
 Period  $\lambda_0 = 22$  mm  
 Number of period  $N=90$   
 $K=1.79$   
 Harmonic  $n=3$



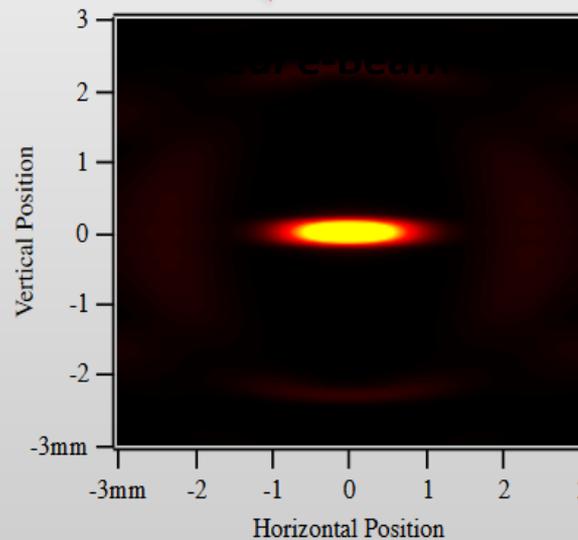
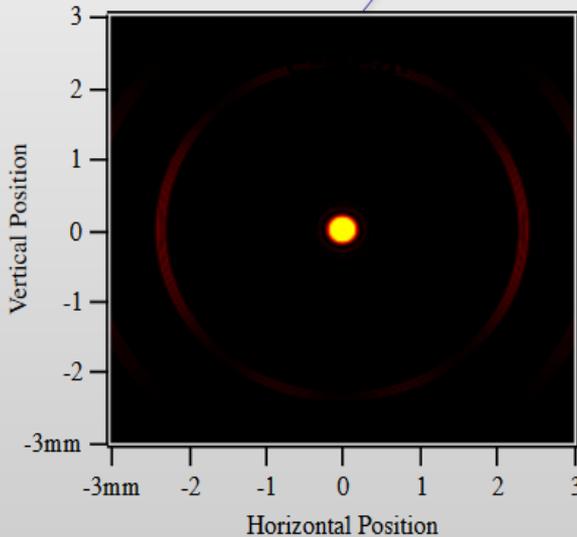
**Undulator resonance wavelength:**

undulator period

magnetic field

$$\lambda = \frac{\lambda_u}{2\gamma^2} \left( 1 + K^2/2 + \gamma^2\theta^2 \right)$$

$e$ -beam energy
 $e$ -beam divergence



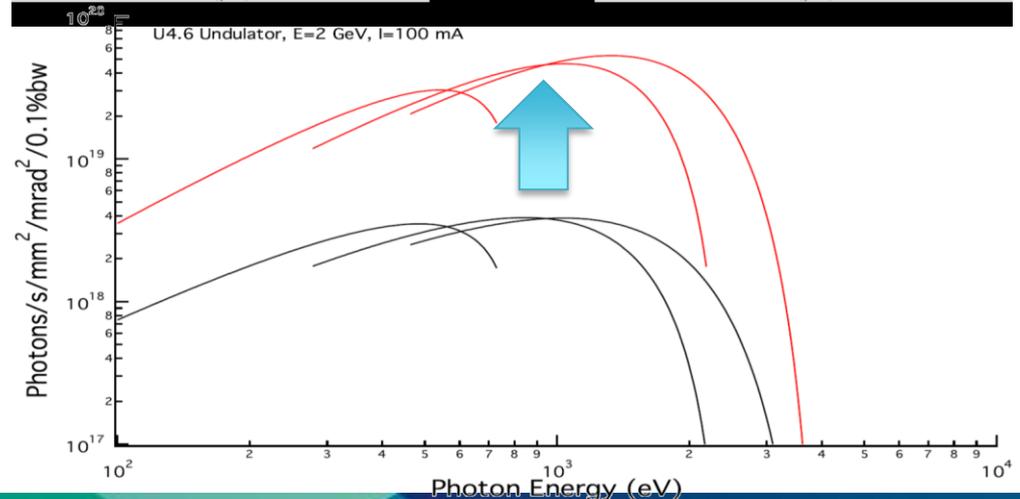
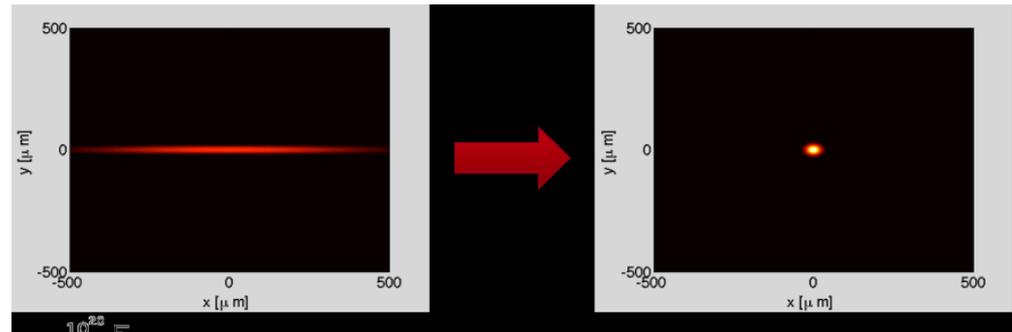
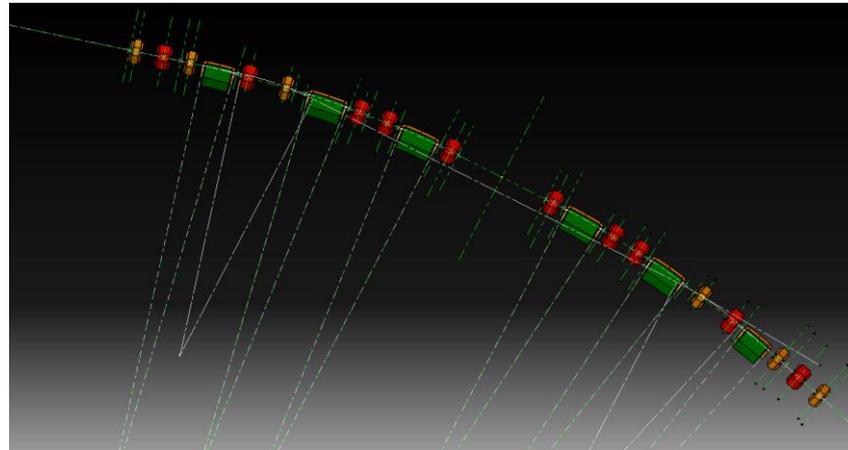
**“undulator parameter”, it is proportional to the undulator magnetic field:  
 $K \propto B$**

# New Generation is Coming

Upgrade of synchrotron light sources is planned worldwide, in order to reach a higher photon brilliance.

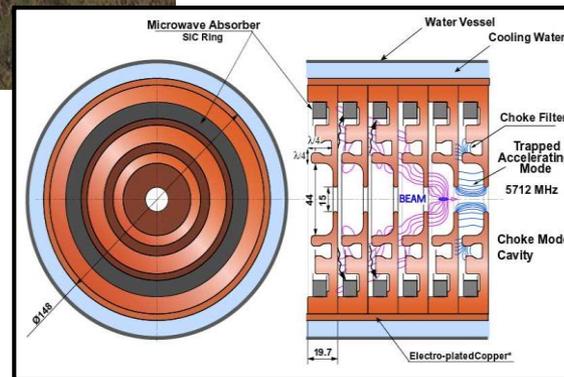
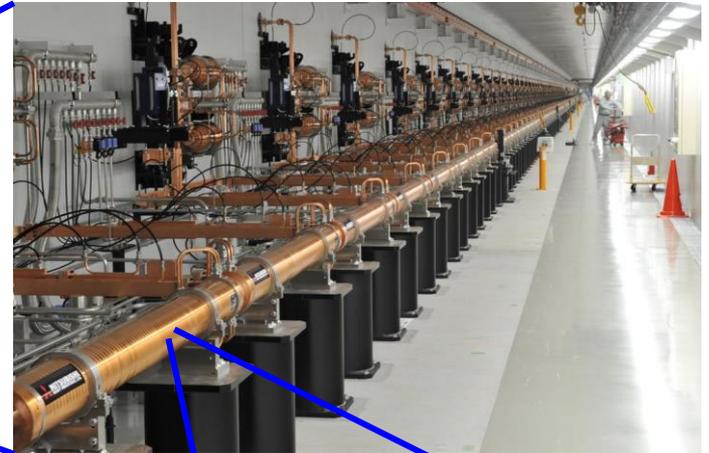
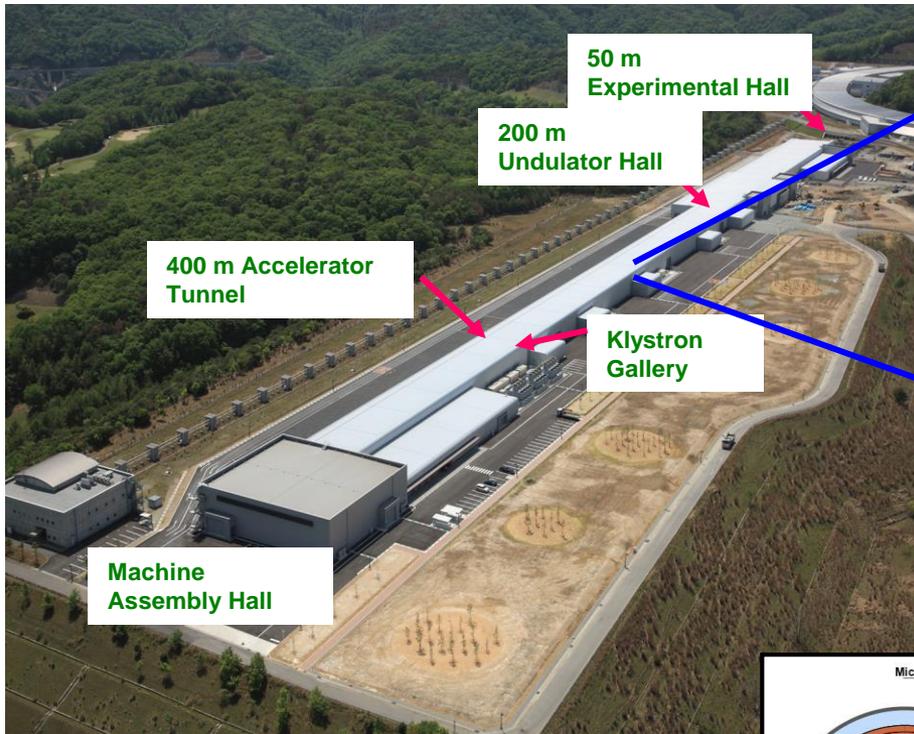
More dipoles, smaller bending angle, smaller e-beam sizes, higher charge density.

*From Elettra to Elettra 2.0:*



# Back Slides Follow

# Radiofrequency Electron Linac

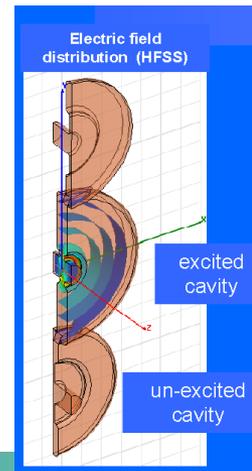
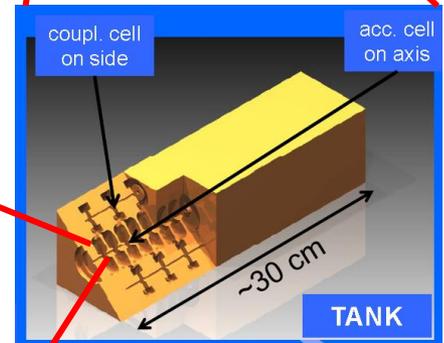
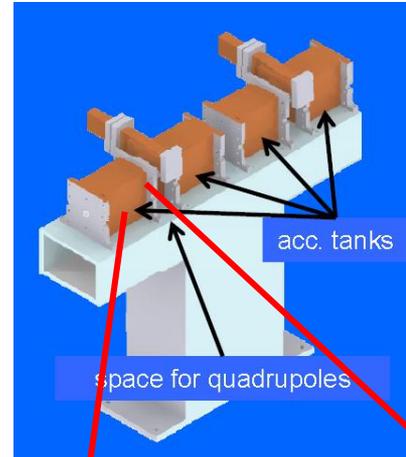
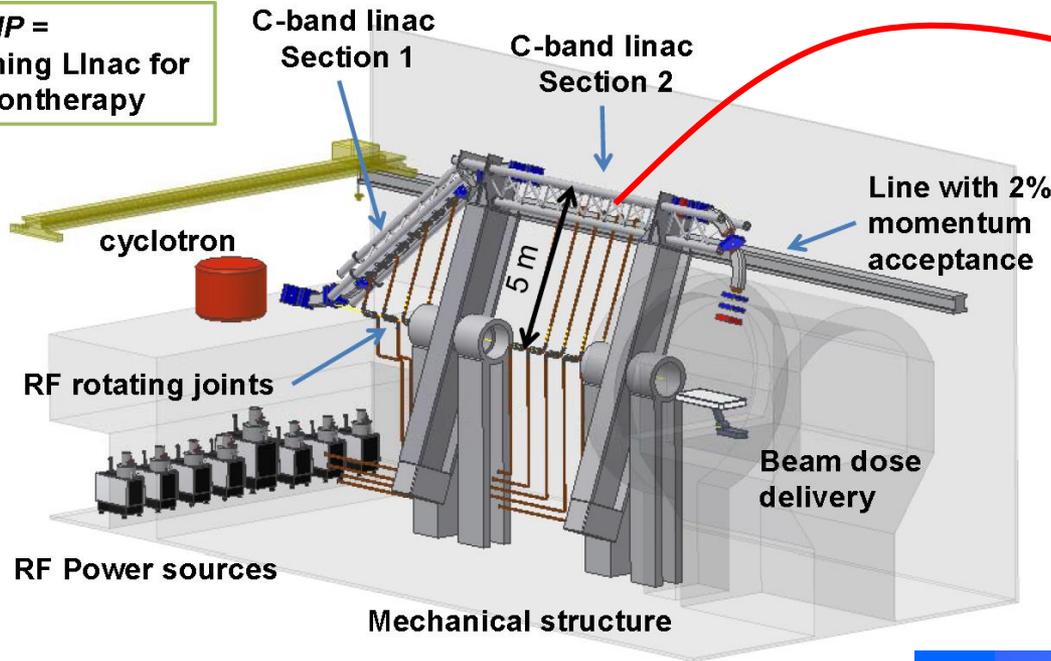


Source: T. Inagaki, T. Shintake

8 GeV e-linac  
 C-band (5.7 GHz)  
 35 MV/m acc. gradient  
 13000 cells mass production

# Radiofrequency Proton Linac

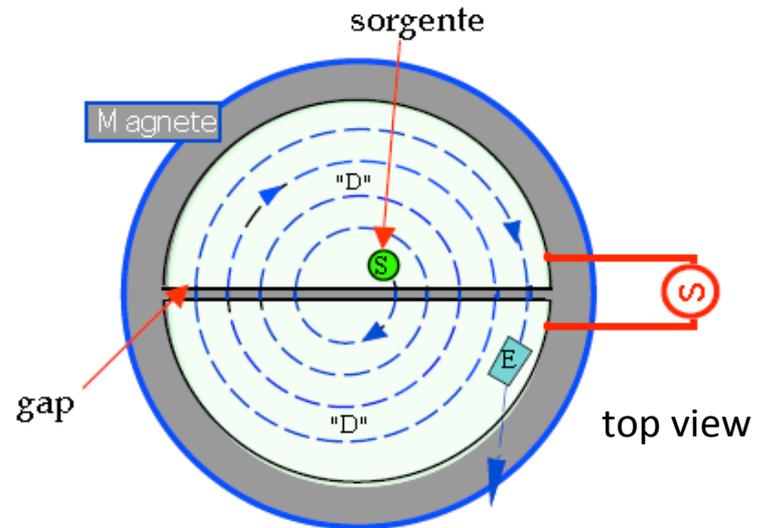
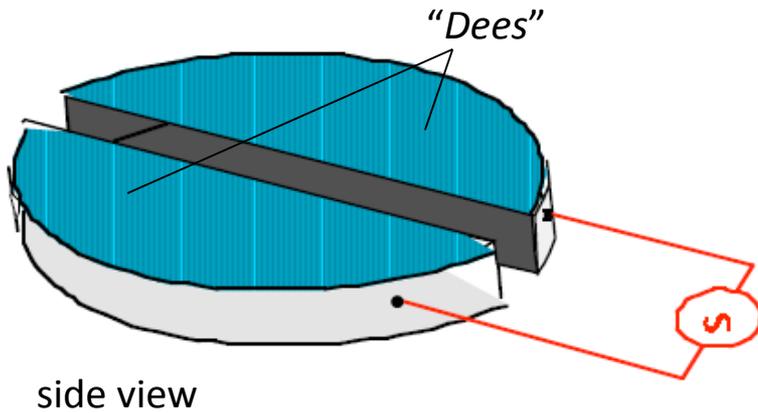
**TULIP =**  
**T**urning **L**inac for  
**P**rotontherapy



Source: A. Degiovanni, U. Amaldi

80–210 MeV p-linac  
 C-band (5.7 GHz)  
 <38 MV/m acc. gradient  
 Rep.rate, 200 Hz

# Cyclotron (E.O.Lawrence & M.S.Livingstone, Berkeley 1931)



$$\left\{ \begin{array}{l} f_{RF} = (2n + 1)f_C \quad \text{Synchronism} \\ \Delta T(t) = qV_o \sin(\omega_{RF}t + \varphi) \quad \text{Energy gain / turn} \end{array} \right.$$

$$\left\{ \begin{array}{l} \rho = \frac{P}{|q|B_o} \quad \text{Lorentz force} \\ P = \sqrt{2m_o T} \quad \text{Classical approximation (e.g., massive particles)} \end{array} \right.$$

- Spiraling motion:

$$\Delta \rho = \rho \frac{1}{2} \frac{\Delta T}{T} = \frac{\Delta T}{|q|cB} \sqrt{\frac{m_o c^2}{2T}}$$

- Maximum kinetic energy:

$$\frac{\sqrt{2m_o T_{\max}}}{|q|B} = R$$

# Sincho- and Sector- Cyclotron

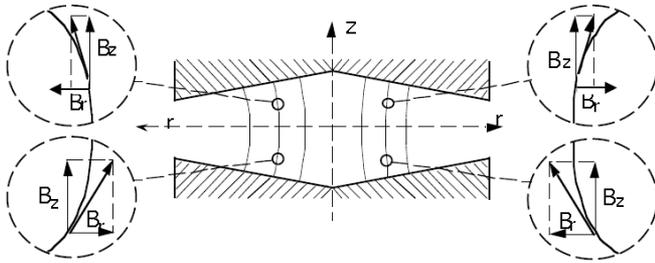
$$\omega_c = \frac{B}{|q|m} = \frac{1}{\gamma} \frac{B}{|q|m_0} \equiv C \omega_{RF}$$

To maintain the synchronism, which ensures the multi/turn acceleration, one has two ways:

1. Increase  $B(t)$  synchronous to  $\gamma(t)$ ,  $\propto \rho(t)$



“sector cyclotron”



TRIUMPH, Canada

2. Increase  $\omega_{RF}(t)$  synchronous to  $\gamma(t)$



“sincro-cyclotron”

N.B.: here the beam is **bunched**, over one period of modulation of  $\omega_{RF}$  !!

CERN SC

